Math 3206 Test 1 – Unit 3: Exponential Functions

Name:___

Part 1: Multiple Choice

{24 marks}

1 Which sequence below represents an exponential sequence?

- A) {2, 6, 10, 14, 18,...}
- B) {3, 5, 9, 16, 24, ...}
- C) $\{4, 8, 24, 96, \dots\}$
- D) $\{256, 64, 16, 4, \ldots\}$

2 Which equation represents a geometric sequence?

- A) y = 2x + 3
- B) $y = x^2 + 5x 6$
- $C) \qquad y = x^3 1$
- D) $y = 4^x + 3$

3 Which equation below will produce a decay curve?

A) $y = 3^{x} - 4$ B) $y = 2(4)^{x}$ C) $y = \frac{1}{2}(3)^{x}$ D) $y = 6(\frac{1}{2})^{x}$

4 What is the equation of the relationship below?

x -2		0	2	4	
У	8	24	72	216	

A) $y = 8(3)^{x/2}$ B) $y = 8(\frac{1}{3})^{x}$ C) $y = 24(3)^{x}$ D) $y = 24(3)^{x/2}$

For the equation below $y = 2.5^x - 6$, answer questions 5 to 7.

5 What is the equation of the horizontal asymptote?

- A) y = -6
- B) y = -3.5
- $\mathbf{C} \qquad \mathbf{y} = \mathbf{0}$
- D) y = 2.5
- 6 What is the y-intercept of the graph?
 - A) -6
 - B) -5
 - C) -3.5
 - D) 2.5

7 What is the range of the function?

 $A) \qquad \{x | x > -6, x \in R\}$

 $\mathbf{B} \qquad \{x \mid x > \mathbf{0}, x \in R\}$

 $\{y|y > -6, y \in R\}$ C)

D) $\{y|y > 0, y \in R\}$

A coffee is sitting on Mr. Hunt's desk cooling. It cools according to the function $T = 70(0.80)^{x} + 20$, where x is the time in minutes and T is the temperature in degree Celsius.

What is the initial temperature of the coffee?

- A) 20 70
- B)
- 75 C) D) 90
- 9

Using your function in question 8, what is the temperature after 10 minutes?

- A) 7.5 B) 20
- 27.5 C)
- D) 76
- Using your function in question 8, what will the coffee eventually cool to? 10
 - 0 A)
 - B) 20
 - C) 70
 - D) 90
- 11 Michael invested \$5000 into an account that has a 5.5% annual interest rate. What equation best describes this investment after *t* years?
 - $A = 5000(.055)^{t}$ A)
 - $A = 5000(1.055)^{t}$ B)
 - $A = 5000(1.55)^{t}$ C)
 - D) $A = 5000(.945)^{t}$
- 12 A photocopier is purchased for \$5200 and depreciates in value by 15% per year. Which equation best describes the value of the photocopier in t years?
 - $y = 5200(0.15)^{x}$ A)
 - $y = 5200(0.85)^{x}$ B)
 - $y = 5200(1.15)^{x}$ C)
 - $y = 5200(1.85)^{x}$ D)

Part II

The following formula will be needed to complete this section of the exam.

$$y = ab^x \qquad \qquad y = ab^{x/c}$$

- 1 Each sequence below is geometric. Determine the missing terms by finding the common ratio and using it to find the missing terms of the sequence. {4}
 - A) {8, 17.6, _____, , ____, ...} CR = _____

8

- B) { _____, ____, 102.4, 256} CR = _____
- 2 Using one of the formulas above, write an equation that will represent the exponential data given below. {12}

A)

0	1	2	3	4
15	60	240	960	3840

B)

	0	3	6	9	12
	0.5	4	32	256	2048
C)					

-10	-6	-2	0	4
625	125	25	5	1

D)

i)

F)_____

10	0	20	5	15
54	6	486	18	162

3 For each function

 $y = 2.5^{x} - 6$

below fill in the table of values below

B) identify the exponential function as growth or decay curve

- C) identify the common ratio
- D) identify the y-intercept
- E) state the equation of the asymptote (**show on graph as well**)
- F) state the domain and range
- G) find y(-3)

A)

{12}







G) y(-3) =

i)
$$y = 3(0.60)^x$$



4 State the equation of the horizontal asymptote, y intercept, whether the curve represents growth or decay, and the domain and range. {10}

A)	$y = 4(1.0026)^x$]	B)	$y=5^x-8$

- 5 For each problem below, set up an exponential model and use it to solve the problem. {12}
 - A) Suppose a \$125 000 piece of machinery is depreciating at 8.5% a year. How much will it be worth after 3 years?
 - B) The population of a small town is decreasing at a rate of 7% per year. If the town's population is 12 250 now, what will be the population in 10 years?

- C) The population of black flies in Labrador in the summer grows at a rate of 50% <u>every two days.</u> If there are 5000 flies on June 5, how many flies will there be on June 21?
- 6 Tommy bought a new sports car for \$45 000. It depreciates annually by 20% per year.

	A) Fill in the table below:						{2}
y	year	0		1	2	3	4
value	e of car \$	45 00)0				
	B) What is the common ratio?						
	C) What is the exponential function that describes the above data?						
	D) Using c, find how much will the car be worth in 6 years (show work						rkings). {2}
	E) (Jse your cal	culator to t	find when i	t will be worth	\$10 001?	{2}
7	A cup of coffee is left to cool inside a room and its' cooling can be described function $y = 85(.75)^{x/5} + 15$ where x is time in minutes and T is the te the coffee in degrees Celsius.						bed by the temperature of {3}
	(4 ¹	0	5	10	15	20
	x (time) 0 5 10 15 T (Temperature) 10 15 10 15						
	B) What is the initial temperature of the coffee?						{2}

- C) Enter the function in your calculator and determine when the coffee will be at 50° C? 20° C? $\{4\}$
- D) What will the temperature of the coffee eventually cool to and why? {3}

E) Sketch a graph of the coffee cooling using your table above. Include the horizontal asymptote. {5}

