# Static Equilibrium and Torque

# Section 1: Static Equilibrium I - Balancing Forces

<u>Statics</u> - the physics of keeping objects still by applying forces on them in the appropriate places.

- An object is static equilibrium has no translational motion and no rotational motion.

Hence, all applied forces lead to zero velocity and zero acceleration.

To acquire static equilibrium, we need to know

- what forces must be applied and
- where the force or forces must be applied.

Every object has a point where its mass and weight appear to be concentrated. This point is called the **centre of mass (CM) or the centre of gravity (CG)**. The cat in the picture is "balanced" when the supporting string falls in line with the white dot, which is its CM and CG.



### Section1\_Balancing\_Forces\_soln.notebook

To achieve static equilibrium, 2 conditions must be met:

- 1.  $F_{net} = 0$ , ie å  $F_x = 0$ , and å  $F_y = 0$ , where  $F_{net}$  is the sum of all forces acting through the cente of mass. If  $F_{net} = 0$ , then there is no translational acceleration or motion.
- 2.  $T_{net} = 0$ . If  $T_{net} = 0$ , then there is no rotational motion.

#### Example 1

In the picture to the right the cat is pushing with its front legs and back legs. The front legs cause a forward force of  $F_f = 25 \text{ N} [60^\circ$ above the horizontal], and the back legs cause a forward force of  $F_b = 45 \text{ N} [30^\circ \text{ above the}$ horizontal]. What must be the magnitude and direction of the equilibrium force ( $F_e$ ) applied by you in order to maintain static equilibrium?



equilibrium force => equal in magnitude but opposite in direction to the net form.



In the picture to the right the CG of the piece of art is directly under the point where the supporting strings are attached. The hanging picture weighs 72 N and each of the supporting strings makes an angle of 20° with the frame.



What is the tension in each string? Picture 1s in static equilibrium: so Firet=0. ie E Flogt = Efright + E Fup = E Form Firet= Fright @ Fup = Form Tix = Tax Tiy + Tay = Fg aTy = Fg aTy = Fg blc both strings are acting at the some T = Fg asin0 T = 10N Second Method: Since the strings make the same angle with the picture, the Emission of the supports

hall	weight	
<b>トナドイ</b> ク	- 7.6	$= \frac{1}{2} (72N) = 36N$
20 20'	T 15+9	
	3	$\sin 20^\circ = 36N$
J Fa	T 36 N	T= 36N . 110N
V B	200	$T = \frac{36N}{sinzo} \cdot 110N$
		~~~
		٥

## Example 3

In the picture to the right the CG of the piece of art is directly under the nail that supports it. The hanging picture weighs 7PN and the supporting = T, string forms an isosceles triangle with the frame as shown. What is the tension in the string?  $F_9 = 2T \sin 0$  $73N = 2T \sin 20$ 10N = T

The following set of forces act on a common point:  $F_1 = 55 N$  $F_2 = 45 \text{ N} [15^\circ \text{ W of } \text{N}]$ . What additional force [due E] and is needed to maintain static equilibrium? 15 W of N \_ f2= 45N [N 15° W] F2x = 45N cos 75 : 11.6N [W] Fox = 45N sin 75° = 43.5N[N] Ex= 11.6N [W] + 55N [E] - 43.4N [E] Ey=43.5N [N]  $\int_{1}^{1} 43.5N F_{Net}^{2} = (43.5N)^{2} + (43.4N)^{2}$ For  $F_{Net}^{2} = 61N [E45^{\circ}N]^{2}$ 43.4N  $f_{eq} = 6IN \left[ w45^{\circ}s \right]$ tan 0 = 4<u>3.5</u> 43.0 8- 45

## Example 5

Our intrepid physics student has gotten himself in trouble again. He has manage to get his ATV halfway up a ramp and realizes that he needs help.

With the aid of friction caused by a flat tire he rest = restjust manages to hold the machine steady. The coefficient of static friction is 0.22 and the ATV has a mass of 250 kg. What is the tension in the rope?

$$F_{Net=} T + F_{f} - F_{II}$$
  
 $O = T + \mu mg \cos 20 - mg \sin 0$   
 $O = T + (0.22)(250)(9.8)(0525 - (250)(9.8)sin 25^{\circ})$   
 $T = 550N$ 

A boom set-up for weighing very large fish is shown in the picture. The boom can withstand a compression force of  $3.0 \times 10^3$  N. What is the mass of the largest fish that can be weighed?



Setting up an FBD for the boom will introduce unnecessary info. It is sufficient to consider the force at the top of the boom.,



A bag of clothespins hung in the middle of a 3.00 m clothesline causes the line to dip 1.5° below the horizontal at each end.

a) Draw a free body diagram for this situation.



b) How far does the center of the line dip when the bag of clothespins is hung on it? find x in (a)



- Sin 1.5° = <u>)(</u> 1.5m X= 0.039m X= 3.9cm
- c) What is the mass of the bag of clothespins if the tension in the line is 85.0 N?



$$F_{up} = F_{down}$$

$$\frac{\partial T_{g}}{\partial T_{g}} = F_{g}$$

$$\frac{\partial T_{sin0}}{g} - \frac{mg}{g}$$

$$\frac{\partial (85N) \sin 1.5^{\circ}}{9.8m / s^{2}} = M$$

Lab - Shatic Equilibrium p. 272  
T.= 2.944  
T.= 2.944  
T.= 2.944  
T.= 2.944  
T.= 2.944  
T.= 2.94N  
Tension in the strings is provided by  
the force of gravity.  
\* Purpose of Lab: Show that the masses are  
in static equilibrium  
Strat: Find F.g for each mess This is the tension  
in each string.  
F.g.: (0.3 Kg)(9.8 m/s<sup>2</sup>) = 2.94N  
F.g.: 2.94N  
F.g.: (0.3 Kg)(9.8 m/s<sup>2</sup>) = 1.96N  
To show static equilibrium show that  

$$E Fieft = E Fright d E Furp - E Fabura.$$
  
Tix = 2.94N cos 24° = 2.69N (L)  
Ty , 0.94N sin 24° = 1.20N (O)  
Tax = 2.94N cos 65° = 1.24N (R)  
Tay = 2.94N sin 65° = 2.66N (D)  
Tsx = 1.96N cos 47° = 1.34N (R)  
Tsy = 1.96N sin 47° = 1.43N (O)  
E Tieft = 2.69N  
E Tright = 2.69N  
E Tright = 2.69N  
E Tright = 1.24N + 1.34N = 2.58N  
AT = 0.11N (1.94) - Source of errors  
- Should be zero  
E Tup = 1.20N + 1.43N = 2.63 N

In the figure below, the pulleys are frictionless and the system is in static equilibrium. If Fg1 = 200.0 N, find the weight of object 2 and 3.



Find the tension in each string.



# Example 10 Find the tension in each string. 30 Ť,x 40.0 N 2Fx=0 & Fiett = & Fright $T_1 x = T_{2x}$ $T_{1} \cos 30^{\circ} = T_{2} \cos 50^{\circ}$ $T_1 = \frac{T_a \cos 60}{\cos 30^6}$ T.= 0.5774 T. EFy=0 EFup=Efdown $T_{i}y + T_{2}y = T_{3}$ $T_{i}s_{i}s_{0}^{\circ} + T_{2}s_{i}s_{0}^{\circ} = 40\lambda$ $(0.5774T_{2})$ sin 30 + T<sub>2</sub> sin 60 = 40N 0.2887 Tat D.8660Tz= 40N 1.1547T, = 40N T2= 34.6N J.= 0.571412 = 0.5774(34.6N) 20.01

#### 10