Section 1.5: Graphing Accelerated Motion

In this lesson you will

- Construct d-t and v-t graphs for an object undergoing uniformly accelerated motion.
- Use the d-t graphs to determine the instantaneous and average velocity.
- Use the v-t graphs to determine the displacement of the object during any specific time interval.
- Use the v-t graphs to determine the acceleration of the object.
- Describe the motion of an object given its displacement-time graph or velocity-time graph.
- Compare and contrast displacement vs. time and velocity vs. time graphs.

Recall:

Uniform Motion

- 1. <u>Position-time graph (Displacement-time graph)</u>
 - The **position vs. time** graph for uniform motion is linear. (a diagonal line or a horizontal line)
 - The slope of the line represents the velocity.
 - If the slope is positive: moving to the right at a constant speed
 - If the slope is negative: moving to the left at a constant speed.
 - If the slope is 0: the object is at rest.
 - The y-intercept of the graph represents the initial position.
 - 2. <u>Velocity-time graph</u>
 - The velocity vs. time graph for uniform motion is a horizontal line.
 - The y-intercept of the graph presents the average velocity.
 - If the graph is in the first quadrant, the object is moving to the right.
 - If the graph is in the fourth quadrant, the object is moving to the left.
 - The **area** "under" any part of a v-t graph (between the x-axis and the time axis) represents the displacement for that time interval.
 - If the area is above the time axis: positive displacement
 - If the area is below the time axis: negative displacement
 - Average velocity = area ÷ time

Accelerated Motion

- 1. <u>Position-time graph (Displacement-time graph)</u>
- The position-time graph for uniform acceleration is parabolic. (curved line)
- The slope of the line tangent to the curve represents the instantaneous velocity.

To construct a tangent to a curve:

- 1 Choose a point on the curve.
- 2 Draw a straight line parallel to the direction of the curve at that point. The line touches the curve at that point only: and the angles between the curve and the line on either side of the point are equal.
- 3 Then draw a rise-run triangle and calculate the slope.



 The slope of the line that joins two points on the curve represents the average velocity.

Find Vav between B+C. Vav = <u>54m-10m</u> B(1.5s, 10m) C(3hesy-intercept of the graph represents the initial position.

2. <u>Velocity-Time Graphs</u>

- The v-t graph for uniform acceleration is a diagonal line.
- The slope of the line represents the acceleration of the object.
- The y-intercept represents the initial velocity.
 - If the graph is in the first quadrant, the object is moving to the right.
 - If the graph is in the fourth quadrant, the object
 is moving to the left.
- The **area** "under" any part of the graph (between the x-axis and the time axis) represents the displacement for that time interval.
 - If the area is above the time axis: positive displacement
 - If the area is below the time axis: negative displacement
- Average velocity = area ÷ time
- The **v-t** graph for <u>non-uniform acceleration</u> is a parabolic curve.
- The **slope** of the line or the slope of the line tangent to the curve gives the instantaneous acceleration of the object.

Note: Important

If velocity and acceleration are in the same direction (same signs), the object is speeding up.

If velocity and acceleration are in opposite directions (opposite signs), the object is slowing down.

Therefore:

- 1 If v is + and a is +: object is moving to the right and speeding up.
- 2 If v is and a is -: object is moving to the left and speeding up.
- 3 If v is + and a is -: object is moving to the right and slowing down.
- 4 If v is and a is +: object is moving to the left and slowing down.

Examples:

- 1. To the right is a graph of a section of a roller coaster ride.
 - a) Find the instantaneous velocity at 0 s, 3.0 s and 5.0 s.



To find the instantaneous velocity we need to draw tangents to the graph at 0 s, 3.0s, and 5.0s and then find the slope of each.



b) Find the average velocity of the roller coaster between 0 - 3.0 s, and 3.0 s - 5.0 s.

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Average velocity = slope of the line joining two points.
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$$\frac{0-3s}{V_{AV}} = \frac{62m}{3s} = 20.7m/s = 21m/s$$

$$\frac{3-5s}{2s} = \frac{3s}{2s} = 20.7m/s = 21m/s$$

$$\frac{3-5s}{2s} = \frac{3s}{2s} = \frac{3s}$$

d) Sketch a graph of the corresponding v-t graph.



2. A) Describe the motion of the following objects.

ii)



j)



B) Sketch the corresponding velocity-time graphs.



3. Draw a position-time graph to represent a ball falling from the top of a building. Draw the corresponding velocity-time graph.





- b) Find the displacement of the car in 5.0 s. $d = area = \frac{1}{2}bh = \frac{1}{4}(5.0 f)(20 m) = 50 m$
 - c) Describe the motion of the car. The car is moving to the right + speeding up.

 The v -t graph at the right represents a a cyclist's motion.





a) Find the cyclist's acceleration for each section.

A:
$$a = \frac{-20m|s}{4.0s} = -5.0m/s^{2}$$

iC: $a = \frac{-20m|s}{4.0s} = -5.0m|s^{2}$
b) Find the cyclist's total displacement.
 $A_{1} = \frac{1}{2}bh = \frac{1}{2}(4.0s)(20m/s) = 40m$
 $A_{2} = \frac{1}{2}bh = \frac{1}{2}(4.0s)(-20m/s) = -40m$
 $\vec{d}_{7} = 0m$

- c) Describe the cyclist's motion.
- A: cyclist is driving up hill & slowing down. B: stops & changes direction C: moving down hill & speeding up.

acceleration at 4.0 s? $\vec{v} = 0 m/s$ $a = -5.0 m/s^2$

6. Using the velocity -time graph below, answer the following questions.



Overview of d-t Graph Manipulations



Graph Analysis for a v-t graph



Summary of d-t Graph Analysis



Determining the Action of an Object



Speeding up

d - †	v -t	velocity	acceleration	
		v > 0	<i>a</i> > 0	R
		$\vec{v} < 0$	<i>a</i> < 0	-

Slowing Down

d-tv-tvelocityaccelerationiiiiiiiiiiiiiiiiiiii