Unit 2: Quadratics

Section 2.1: Linear Versus Non-Linear Function Applications Introduction to Parabolic Curves

Example: A ball is shot from a cannon into the air and its path can be recorded according to the data in the table below.



A) Using your knowledge of sequences and patterns determine algebraically whether a linear, quadratic, or cubic equation should describe the pattern.



B) Determine the equation of the curve of best fit. (TI-83 Plus)

 $y = ax^{2} + bx + c$ a = -5 $y = -5x^{2} + 40x$ b = 40H(t)=-5t²+40t / height after tim t seconds time

Section2.1_Introduction_to_Parabolic_Curves_Soln.notebook

C) Using your curve of best fit, determine the height the cannon ball at 2.5 s? 5.5 s? (Two ways)

 $H(t) = -5t^{2} + 46t$ $H(2,5) = -5(2,5)^2 + 40(2,5)$ H(2.5) = -5(6.25) + 100H(2,5) = -31.25 + 100 $(\frac{H(2.5)}{This means that He height at 2.5s is})$ $H(5.5) = -5(5.5)^2 + 40(5.5)$ H(5.5) = -5(30.25) + 220H(5.5) = -151,25+220H(5.5) = 68.75mUse "Trace" on your calculator to find the height at 2.55 & 5.55 you will get the same answer Steps Trace [1] (y=-5x2+40x should be at the top of the screen). Then type X= 2.5s [entir you will see y= 68.75. This is your height at 2.5s. Repeat for 5.55. D) Use your calculator to determine the vertex of the parabola. (Recall, the vertex is the highest or lowest point on the graph.) V(4,80) (Maximum) 2nd Iltrace <u>4:maximum</u> -> go to the left of the maximum (entro), go to the right of maximum and enter Guess? enter V(4,80) The value of the max/min minmax The vertex means: At 4s, the maximum height is 80m

E) When is the ball at its maximum height? (Use Vertex)
4 Seconds
5) What is the maximum height of the ball? (Use Vertex)
80 m
80 m
9 - coordinate
(2nd one)

G) When will the ball hit the ground?
Sheight is Om
Need to find when the height
Of the ball is Om.
> use (trace) on the calculator
find the value of "X" when Y=0.

Answer: 8s

All of these questions lead to the discussion of the Parabolic Curve often known as the PARABOLA= graph of a quadratic equation.

Case I

Case II



The General Form of any Quadratic Equation is:

$$y = ax^2 + bx + c$$

Case I = a > 0

Case II = a < 0

In other words, **a** is positive.

graph opens upward Vertex is a minimum In other words, **a** is negative.

graph opens downward vertex is a maximum

Graphing Quadratic Functions

The Base Graph is always $y = x^2$. All parabolas are compared to this graph.

The graph of $y = x^2$ has the following Table of Values:



✻ Important notes on $y = ax^2 + bx + c$ (+) if a > 0, the parabola opens upwards (minimum vertex) V_{ν} 1 if a < 0, the parabola opens downwards (maximum vertex) 2 3 the form is called general form the vertex is always found by using the formula $x = \frac{-b}{2a}$ 4 This is always the x-coordinate of the vertex. To get the *y*-coordinate of the vertex you substitute the *x*-coordinate of the vertex into the quadratic equation and solve for y. For each quadratic equation determine **Example:** -A) the direction of the opening of the parabola B) the coordinates of the vertex - C) the type of vertex i) $y = 3x^2 - 12x + 1$ A) a=3 : it opens upward (V) C) Vertex is a minimum B) X=-b (-b means use the apposite of x= 12 3(3) X= 2 X= 12 To find the y-coordinate, sub x=2 into equation. $y = 3x^2 - 13x + 1$ $y = 3(2)^2 - 12(2) + 1$ y= 3(4)-24 + 1 y= 12-24 + 1 y= -11 Vertex (2,-11)

ii)
$$y = 8x^{2} \pm 16x$$

A) $a = 8$, it opens upward (U)
c) Vertex is a minimum
(b) $x = -\frac{16}{2a} = -\frac{16}{2(8)} = -\frac{16}{16} = -1$
 $y = 8x^{2} + 16x$
 $y = 8x^{2} + 16x$
 $y = 8(-1)^{2} + 16(-1)$
 $y = -8$ $V(-1)^{-8}$
iii) $y = -x^{2} \pm 10x - 2$
A) $a = -1$, \therefore it opens downward
c) Vertex is a maximum.
(b) $x = -\frac{10}{2a} = -\frac{10}{2(-1)} = -\frac{10}{-2} = 5$
 $y = -x^{2} + 10x - 2$
 $y = -(25) + 50 - 2$
 $y = -25 + 50 - 2$
 $y = 23$ $V(5, 23)$
iv) $y = -4x^{2} \pm 16x + 3$
A) $a = -4$, opens down (1)
(c) Vertex is a maximum
(c) Vertex is a maximum
(c) $y = -4x^{2} \pm 16x + 3$
 $y = -16 \pm 32 \pm 3$
 $y = 19$
 $V(2, 19)$