Section 2.3: Applying Quadratic Relationships and Maximum and Minimum Problems

We now begin applications of graphing parabolas.

By the end of this section you should be able to:

- 1 Determine if a relationship is quadratic (D2)
- 2 Find the equation of the parabola (curve of best fit) in your TI-83
- 3 Find the equation of the quadratic function.
- 4 Find the vertex of the quadratic function
- 5 Interpret your vertex as a solution to a maximum or minimum problem

Recall,

To find the vertex, use $\frac{-b}{2a}$ to find the x-coordinate and then substitute this value into $y = ax^2 + bx + c$ to find the y-co-ordinate.

Applying Quadratic Relationships

- 1. Squares are joined together to make rectangles whose areas are recorded in the table. Each square's length and width are consecutive whole numbers.
 - A) Complete the table and extend the pattern by drawing rectangles on graph paper.



B) Find the sequence of first and second level differences, D_1 and D_2 , for the area section of the table.



- C) Explain whether there is a linear or quadratic relationship. Quadratic because Dz is constant.
- D) Using your TI-83 create a scatter plot and find the equation of the curve of best fit. b = 1 c = 0 $y = 1x^2 + 1x$ $y = x^2 + x$
- E) Use your equation of the curve of best hit to = X determine the area of rectangle 25.

Maximum and Minimum Problems Given the Function

- 2. A ball is thrown into the air and its path can be described by the function $y = -4.9x^2 + 29.4x + 1$, where x is the time in seconds and y is height in meters.
 - A) What kind of function is displayed above? How do you know? Quadratic blc you have x^{2"} in the equation.
 - B) What kind of graph will be displayed? What kind of vertex?

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C) Determine the initial height of the ball? (The initial height of the ball occurs at time, i.e x = 0.)

$$y_{=} - 4.9 k^{2} + 29.4 x + \frac{1}{2}$$

$$y_{=} - 4.9(0)^{2} + 29.4(0) + 1$$

$$y_{=} 1$$

D) Determine, algebraically, the maximum height reached by the ball. (Note: this is a max/min problem because it used the term maximum...must find vertex

$$x = \frac{-b}{2a} \quad x = \frac{-29.4}{2(-4.9)} - \frac{-29.4}{-9.8} = 3$$

Therefore,
$$y = -4.9x^{2} + 29.4x + 1$$

 $y = -4.9(3)^{2} + 29.4(3) + 1$
 $y = -4.9(9) + 88.2 + 1$
 $y = -4.9(9) + 88.2 + 1$
 $y = -44.1 + 88.2 + 1$
 $y = -45.1$
 $y = -4.9(9) + 88.2$

Statement: the maximum height was $y = \frac{45.1}{s}$ m at x = 3

- 3. An arrow is shot into the air and its path can be described by the function $h(t) = -5t^2 + 30t$, where t is the time in seconds and h(t) is the height of the arrow in meters.
 - A) How do you know the arrow was fired from ground level? (In other words, how do you know that the initial height was 0?)

"c" in the equation is O (h(t)=-5t²+30t+0 Since the initial height was O, the arrow was fired from the ground.

 B) Determine algebraically the maximum height reached by the arrow. (Note: this is a max/min problem because it used the term maximum...must find vertex)

$$t = \frac{-b}{2a} = \frac{-30}{2(-5)} = \frac{-30}{-10} = 3$$

h(t) is a fancy name for y therefore: h(3) = $5(3)^{2}+30(3)$ h(3) = -5(9) + 90h(3) = -45 + 90h(3) = 45 (This means: the height at 3s is 45m) 45 = y -coordinate of vertex.